Mathematics

10

Sample Question Paper

Basic (Code 041)

ANSWERS

Section - A

1.	(d)	2.	(<i>a</i>) 3. (C)
4.	(C)	5.	(<i>b</i>) 6. (C)
7.	(d)	8.	(<i>a</i>) 9. (C)
10.	(d)	11.	(<i>a</i>) 12. (b)
13.	(d)	14.	(<i>d</i>) 15. (C)
16.	(a)	17.	(<i>b</i>) 18. (a)
19.	(d)	20.	(<i>b</i>)	

Section - B

21. Let us assume on the contrary that $\sqrt{3}$ is a rational number and its simplest form is $\frac{a}{b}$, where *a* and *b* are integers having no common factor other than 1 and $b \neq 0$.

 $\sqrt{3} = \frac{a}{b}$ *.*.. $3 = \frac{a^2}{h^2}$ [Squaring both sides] \Rightarrow $3b^2 = a^2$ \Rightarrow ...(1) \therefore a^2 is divisible by 3 [:: $3b^2$ is divisible by 3] [:: 3 is prime and divides $a^2 \implies 3$ divides a] \Rightarrow *a* is divisible by 3 Let a = 3c for some integer c. Substituting a = 3c in (1), we get $3b^2 = (3c)^2 \implies 3b^2 = 9c^2 \implies b^2 = 3c^2$ \Rightarrow [:: $3c^2$ is divisible by 3] \Rightarrow b^2 is divisible by 3 \Rightarrow *b* is divisible by 3 [:: 3 is prime and divides $b^2 \Rightarrow 3$ divides *b*] Since, *a* and *b* are both divisible by 3, \therefore 3 is a common factor of *a* and *b*. But this contradicts the fact *a* and *b* have no common factor other than 1.

This contradiction has arisen because of our incorrect assumption that $\sqrt{3}$ is rational.

Hence, $\sqrt{3}$ is an irrational number.

 $\tan (A - B) = \frac{1}{\sqrt{3}}$ 22. $\tan(A - B) = \tan 30^{\circ}$ \Rightarrow $A - B = 30^{\circ}$...(1) \Rightarrow $\sin(A+B) = \frac{\sqrt{3}}{2}$ $\sin(A + B) = \sin 60^{\circ}$ \Rightarrow $A + B = 60^{\circ}$ \Rightarrow ...(2) Adding (1) and (2), we get $2A = 90^{\circ}$ \Rightarrow $A = 45^{\circ}$ \Rightarrow Substituting $A = 45^{\circ}$ in (1), we get $B = 60^{\circ} - A \implies B = 60^{\circ} - 45^{\circ} = 15^{\circ}$ *.*.. or $\cos \theta + \sin \theta = \sqrt{2} \cos \theta$ $\sin \theta = \sqrt{2} \cos \theta - \cos \theta$ \Rightarrow $\sin \theta = (\sqrt{2} - 1) \cos \theta$ \Rightarrow $\cos \theta = \frac{\sin \theta}{\sqrt{2} - 1}$ \Rightarrow $\cos \theta = \frac{\sin \theta}{(\sqrt{2} - 1)} \times \frac{(\sqrt{2} + 1)}{(\sqrt{2} + 1)}$ \Rightarrow $\cos \theta = \frac{\sin \theta \left(\sqrt{2} + 1\right)}{2 - 1}$ \Rightarrow $\cos \theta = \sqrt{2} \sin \theta + \sin \theta$ \rightarrow $\cos \theta - \sin \theta = \sqrt{2} \sin \theta$ Hence, proved. \Rightarrow 23. Distance covered is 1 revolution of wheel

=
$$2\pi r$$

= $2 \times \frac{22}{7} \times \frac{70}{2} = 220 \text{ cm}$

According to the question, required speed of the bicycle = 19.8 km/hr = 5.5 m/s Distance covered by the wheel in 10 seconds

Distance covered by the wheel in 10 seconds

= Number of revolutions × Distance covered in 1 revolution

$$\Rightarrow 55 = \text{Number of revolutions} \times \frac{220}{100} \left[1 \text{ cm} = \frac{1}{100} \text{ m} \right]$$

 $\Rightarrow \text{ Number of revolutions} = \frac{55}{220} \times 100 = 25$

or

- Radius of sector, r = 60 cmAngle of major sector, $\theta = 360^\circ - 90^\circ = 270^\circ$ Perimeter of table top = Perimeter of major sector + 2r $= \frac{\theta}{360^\circ} \times 2\pi r + 2r$ $= \frac{270^\circ}{360^\circ} \times 2 \times \frac{22}{7} \times 60 + 2 \times 60$ = 282.85 + 120 = 402.85 cm
- 24. Let ABCD be the rhombus, whose diagonals AC and BD bisect at O. Diagonals of rhombus bisect each other at right angle.
 Let AC = 50 cm and BD = 120 cm, ∠AOB = 90°

So,
$$AO = \frac{1}{2}AC$$
 and $OB = \frac{1}{2}BD$
 $\Rightarrow AO = \frac{1}{2} \times 50$ and $OB = \frac{1}{2} \times 120$
 $\therefore AO = 25$ cm, $OB = 60$ cm
In right $\triangle AOB$, we have

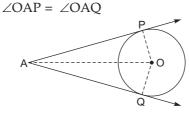
$$AB^2 = AO^2 + OB^2 \implies AB^2 = 25^2 + 60^2 = 4225$$
$$AB = 65$$

Hence, side of the rhombus is 65 cm.

25. **Given:** A circle with centre O and a point A outside it. AP and AQ are tangents drawn to the circle from point A.

To prove:

 \Rightarrow



Proof: In $\triangle OAP$ and $\triangle OAQ$, we have

OP = O	Q [Radii of the same circle]
AP = A	Q [Tangents from an external point are equal]
OA = O	A [Common]
$\Delta OAP \cong \Delta$	DAQ [By SSS congruence]
\therefore $\angle OAP = \angle$	OAQ [CPCT]

Section - C

26. Given that $x + yp^{1/3} + zp^{2/3} = 0$

...(1)

On multiplying both sides by $p^{1/3}$, we get $xp^{1/3} + yp^{2/3} + zp = 0$...(2)

Multiply (1) by y and (2) by z and subtracting, we get $(xy + y^2p^{1/3} + yzp^{2/3}) - (xzp^{1/3} + yzp^{2/3} + z^2p) = 0$ \Rightarrow $(y^2 - xz)p^{1/3} + xy - z^2p = 0$ \Rightarrow $y^2 - xz = 0$ and $xy - z^2p = 0$ [$\because p^{1/3}$ is irrational] \Rightarrow $y^2 = xz$ and $xy = z^2p$ \Rightarrow $y^2 = xz$ and $x^2y^2 = z^4p^2$ \Rightarrow $x^{2}(xz) = z^{4}p^{2}$ \Rightarrow $x^{3}z - z^{4}p^{2} = 0 \implies z(x^{3} - z^{3}p^{2}) = 0$ \Rightarrow $x^3 - z^3 p^2 = 0$ or z = 0 \Rightarrow $p^2 = \frac{x^3}{z^3}$ \Rightarrow $p^{2/3} = \frac{x}{z}$ \Rightarrow This is not possible as $p^{1/3}$ is irrational and $\frac{x}{z}$ is rational. $x^3 - p^2 z^3 \neq 0$ *.*.. Hence, z = 0Putting z = 0 in $y^2 - xz = 0$, we get y = 0Putting y = 0 and z = 0 in (1) \Rightarrow x = 0x = y = z = 0.Hence, 27. Sum of roots (S) = -1Product of roots (P) = -6Required quadratic polynomial $x^2 - Sx + P$ $= x^2 - (-1)x + (-6)$ $= x^2 + x - 6$

28.	Let 1 man can finish the work in <i>x</i> days					
	and 1 woman can finish it in y days.					
	1 man's 1 day's work = $\frac{1}{x}$					
	1 woman's 1 day's work = $\frac{1}{y}$					
	8 men and 12 women can finish the work in 10 days					
	$\Rightarrow (8 \text{ men's 1 day's work}) + (12 \text{ women's 1 day's work}) = \frac{1}{10}$					
	8 12 1	(1)				
	6 men and 8 women can finish the work in 14 days					
	$\Rightarrow (6 \text{ men's 1 day's work}) + (8 \text{ women's 1 day's work}) = \frac{1}{14}$					
	6 8 1	(2)				
	Multiply equation (1) by 2 and equation (2) by 3					
	16 24 1	(3)				
	$\Rightarrow \qquad \frac{18}{x} + \frac{24}{y} = \frac{3}{14} \qquad \dots$	(4)				
	Subtracting (3) from (4)					
	$\Rightarrow \qquad \frac{18}{x} - \frac{16}{x} = \frac{3}{14} - \frac{1}{5}$					
	$\Rightarrow \qquad \frac{2}{x} = \frac{1}{70} \Rightarrow x = 140$					
	From equation (2)					
	$\frac{6}{140} + \frac{8}{y} = \frac{1}{14}$					
	$\Rightarrow \qquad \frac{8}{y} = \frac{1}{14} - \frac{6}{140}$					
	$\Rightarrow \qquad \frac{8}{y} = \frac{4}{140}$					
	\Rightarrow $y = 280$					
	Hence, time taken by man alone to finish the work is 140 days, and time tak	en				

by woman alone to finish the work is 280 days.

or

$$\frac{x}{3} + \frac{y}{4} = 6 \qquad ...(1)$$
$$\frac{x}{6} + \frac{y}{2} = 6 \qquad ...(2)$$

$$\frac{x}{6} + \frac{y}{2} = 6$$
 ...(2)

Dividing equation (1) by 2, we get

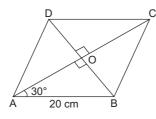
 $\Rightarrow \qquad \frac{x}{6} + \frac{y}{8} = 3 \qquad \dots (3)$

Subtracting equation (3) from equation (2), we get

 $\frac{x}{6} + \frac{y}{2} - \frac{x}{6} - \frac{y}{8} = 6 - 3$ $\frac{y}{2} - \frac{y}{8} = 3$ \Rightarrow $\frac{3y}{8} = 3$ \Rightarrow v = 8 \Rightarrow Substituting y = 8 in equation (1), we get $\frac{x}{3} + \frac{8}{4} = 6$ $\frac{x}{3} + 2 = 6$ \Rightarrow $\frac{x}{3} = 4 \implies x = 12$ \Rightarrow $3y - 2x = 3 \times 8 - 2 \times 12 = 0$ $\frac{x}{y} + \frac{1}{2}$ and

$$= \frac{12}{8} + \frac{1}{2}$$
$$= \frac{3}{2} + \frac{1}{2}$$
$$= 2$$

29. In the given diagonals AC and BD bisect each other at right angles at O.



In right $\triangle AOB$,

$$\sin 30^\circ = \frac{OB}{AB} \implies \frac{1}{2} = \frac{OB}{20} \implies OB = 10 \text{ cm}$$

BD = 2OB \implies BD = 2 × 10 = 20 cm

$$\cos 30^\circ = \frac{AO}{AB} \Rightarrow \frac{\sqrt{3}}{2} = \frac{AO}{20} \Rightarrow AO = 10\sqrt{3} \text{ cm}$$

 $AC = 2AO \Rightarrow AC = 2 \times 10\sqrt{3} = 20\sqrt{3} \text{ cm}$

Hence, length of diagonals are 20 cm and $20\sqrt{3}$ cm.

30. Class size = Difference between any two consecutive mid values = 25 - 15 = 10. Mid values 15 corresponds to class (15 - 5) - (15 + 5), *i.e.* 10 - 20, and so on. Thus, cumulative frequency table for the given data is:

Class Interval	Frequency (f _i)	Cumulative Frequency (cf)
10 – 20	4	4
20 - 30	28	32
30 - 40	15	47
40 - 50	20	67
50 - 60	17	84
60 - 70	16	100
Total	$n = \Sigma f_i = 100$	

Here, $n = \Sigma f_i = 100 \implies \frac{n}{2} = \frac{100}{2} = 50.$

The cumulative frequency just greater than 50 is 67 and the corresponding class is 40 - 50. So, the median class is 40 - 50.

...

$$l = 40, cf = 47, f = 20 \text{ and } h = 10$$

Median = $l + \left(\frac{\frac{n}{2} - cf}{f}\right) \times h$
= $40 + \left(\frac{50 - 47}{20}\right) \times 10 = 40 + \frac{3}{20} \times 10$
= $40 + 1.5$
= 41.5

Hence, the median is 41.5.

 $\angle POQ + \angle POR = 180^{\circ}$

 $\angle POQ + 130^{\circ} = 180^{\circ}$

31.

 $\angle PQO = 90^{\circ}$...(1) [The tangent at any point of a circle is perpendicular to the radius through

the point of contact]

[Straight angle]

$$\Rightarrow$$

In
$$\triangle OPO$$
, we have

 \Rightarrow

$$\angle OPQ + \angle PQO + \angle POQ = 180^{\circ}$$

$$\Rightarrow \qquad \angle 1 + 90^{\circ} + 50^{\circ} = 180^{\circ}$$

$$\Rightarrow \qquad \angle 1 = 40^{\circ}$$

...(4)

$$\angle RST = \frac{1}{2} \angle TOR$$

 $\angle POQ = 50^{\circ}$

[Angle subtended by an arc of a circle at the center is twice the angle subtended by it at any point on remaining part of the circle]

$$\Rightarrow \qquad \angle 2 = \frac{1}{2} \angle POR$$
$$\Rightarrow \qquad \angle 2 = \frac{1}{2} \times 130^{\circ} = 65^{\circ}$$

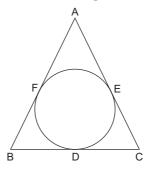
Adding (3) and (4), we get

 $\therefore \qquad \qquad \angle 1 + \angle 2 = 40^\circ + 65^\circ = 105^\circ$

Hence, $\angle 1 + \angle 2 = 105^{\circ}$

or

Since, tangents drawn from an external point to a circle are equal.



BF = BD, CD = CE and AE = AF ...(1)
Semi-perimeter =
$$\frac{AB + BC + CA}{2} = s$$

$$\Rightarrow AB + BC + CA = 2s$$

$$\Rightarrow (AF + BF) + (BD + CD) + (CE + AE) = 2s$$

$$\Rightarrow (AE + BD) + (BD + CE) + (CE + AE) = 2s [:: BF = BD, CD = CE, AE = AF]$$

$$\Rightarrow 2(AE + CE) + 2BD = 2s$$

$$\Rightarrow 2AC + 2BD = 2s$$

$$\Rightarrow AC + BD = s$$

$$\Rightarrow BD = s - AC$$
 Hence, proved.

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Section - D

32. Let total number of birds be *x*.

Then, number of birds moving about in lotus plant = $\frac{x}{4}$.

The number of birds moving on a hill = $\frac{x}{9} + \frac{x}{4} + 7\sqrt{x}$

Number of birds remain on trees = 56

... Number of birds moving in lotus plant + Birds moving on hill

+ Birds remain on trees = Total number of birds $\frac{x}{4} + \frac{x}{9} + \frac{x}{4} + 7\sqrt{x} + 56 = x$ \Rightarrow $\left(\frac{x}{4} + \frac{x}{9} + \frac{x}{4} - x\right) + 7\sqrt{x} + 56 = 0$ \Rightarrow $\left(\frac{9x+4x+9x-36x}{36}\right) + 7\sqrt{x} + 56 = 0$ \Rightarrow $\frac{-14x}{36} + 7\sqrt{x} + 56 = 0$ \Rightarrow Multiply by $\frac{-36}{14}$ $x - 18\sqrt{x} - 144 = 0$ \Rightarrow $\sqrt{x} = v$ Let $y^2 - 18y - 144 = 0$ \Rightarrow $y^2 - 24y + 6y - 144 = 0 \implies y(y - 24) + 6(y - 24) = 0$ \Rightarrow (y + 6) (y - 24) = 0 \Rightarrow y = -6 or y = 24 \Rightarrow $\sqrt{x} = -6$ or $\sqrt{x} = 24$ ·. Since, $\sqrt{x} = -6$ is not possible

Since, $\sqrt{x} = -6$ is not possible \therefore

$$x = (24)^2 = 576$$

Hence, the total number of birds is 576, which is in accordance with problem.

or

The given equation is

 \Rightarrow

$$(x-a) (x - b) + (x - b) (x - c) + (x - c) (x - a) = 0$$

$$3x^2 - 2 (a + b + c)x + (ab + bc + ca) = 0$$

Comparing the given equation with $a_1x^2 + b_1x + c_1 = 0$, we have

$$a_{1} = 3, \ b_{1} = -2(a + b + c), \ c_{1} = ab + bc + ca$$

$$D = b_{1}^{2} - 4a_{1}c_{1}$$

$$= 4(a + b + c)^{2} - 4 \times 3(ab + bc + ca)$$

$$= 4(a^{2} + b^{2} + c^{2} + 2ab + 2bc + 2ca) - 12(ab + bc + ca)$$

$$= 4(a^{2} + b^{2} + c^{2} + 2ab + 2bc + 2ca - 3ab - 3bc - 3ca)$$

$$= 4(a^{2} + b^{2} + c^{2} - ab - bc - ca)$$

$$= 2(2a^{2} + 2b^{2} + 2c^{2} - 2ab - 2bc - 2ca)$$

$$= 2[(a^{2} + b^{2} - 2ab) - (b^{2} + c^{2} - 2bc) + (c^{2} + a^{2} - 2ca)]$$

$$= 2[(a - b^{2}) + (b - c)^{2} + (c - a)^{2}]$$

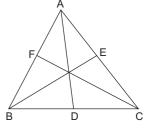
$$[\because (a - b)^{2} \ge 0, (b - c)^{2} \ge 0, (c - a)^{2} \ge 0]$$

As, $D \ge 0$, roots of the given equation are real. For equal roots

D = 0 $\Rightarrow \quad (a-b)^2 + (b-c)^2 + (c-a)^2 = 0$ $\Rightarrow \quad a-b = 0, b-c = 0, c-a = 0 \quad \Rightarrow \quad a = b = c$ $\Rightarrow \quad a = b, b = c, c = a$

Hence, the roots are equal only when a = b = c.

33. **Given:** In $\triangle ABC$, AD, BE and CF are medians. **To prove:** $3(AB^2 + BC^2 + CA^2) = 4(AD^2 + BE^2 + CF^2)$ **Proof:** Since, in any triangle, sum of squares of any two sides is equal to twice the square of half of the third side together with twice the square of the median bisecting it.



...(3)

Therefore, we have,

$$AB^2 + AC^2 = 2(AD^2 + BD^2)$$
 ...(1)

$$BC^{2} + AB^{2} = 2(BE^{2} + CE^{2}) \qquad ...(2)$$

and

Adding the corresponding sides of equations (1), (2) and (3), we get

 $CA^{2} + BC^{2} = 2(CF^{2} + AF^{2})$

$$2(AB^{2} + BC^{2} + CA^{2}) = 2(AD^{2} + BD^{2} + BE^{2} + CE^{2} + CF^{2} + AF^{2})$$

$$\Rightarrow AB^{2} + BC^{2} + AC^{2} = AD^{2} + BE^{2} + CF^{2} + \left(\frac{BC}{2}\right)^{2} + \left(\frac{AC}{2}\right)^{2} + \left(\frac{AB}{2}\right)^{2}$$
[:: AD, BE and CF are medians :: $BD = \frac{1}{2}BC$, $CE = \frac{1}{2}AC$ and $AF = \frac{1}{2}AB$]
$$\Rightarrow AB^{2} - \frac{AB^{2}}{4} + BC^{2} - \frac{BC^{2}}{4} + CA^{2} - \frac{CA^{2}}{4} = AD^{2} + BE^{2} + CF^{2}$$

$$\Rightarrow \frac{3}{4}AB^{2} + \frac{3}{4}BC^{2} + \frac{3}{4}CA^{2} = AD^{2} + BE^{2} + CF^{2}$$

$$\Rightarrow 3(AB^{2} + BC^{2} + CA^{2}) = 4(AD^{2} + BE^{2} + CF^{2})$$

34. Let R be the radius and H the height of the cylindrical tank. Then radius (R) of tank = $\frac{10}{2}$ m = 5 m and H = 2 m \therefore Volume of cylindrical tank = $\pi R^2 H$

$$= \pi \times (5)^2 \times 2 \text{ m}^3$$
 ...(1)

Rate of flow of water through the pipe

$$= 6 \text{ km/h} = \frac{6 \times 1000}{60} = 100 \text{ m/min.} \qquad ...(2)$$

Let r be the radius of the cross-section of the pipe

$$=\frac{20}{2}=10$$
 cm $=\frac{1}{10}$ m

Area of cross-section of the pipe = $\pi r^2 = \pi \left(\frac{1}{10}\right)^2 m^2$

Volume of water flowing through pipe in 1 minute

$$= \pi \left(\frac{1}{10}\right)^2 \times 100 \text{ m}^2 \qquad \text{[using (2)]} \qquad ...(3)$$

Suppose the tank gets filled in *x* minutes.

$$\begin{bmatrix} \text{Volume of water flowing through} \\ \text{pipe in } x \text{ minutes} \end{bmatrix} = \begin{bmatrix} \text{Volume of water} \\ \text{in fill tank} \end{bmatrix}$$
$$\Rightarrow \quad \pi \left(\frac{1}{10}\right) \left(\frac{1}{10}\right) (100) \times x = \pi (5)^2 (2)$$
$$\Rightarrow \quad \pi \times \left(\frac{1}{10}\right)^2 (100) \times x = \pi \times (5)^2 \times 2 \qquad \text{[Using (1) and (3)]}$$
$$\Rightarrow \qquad x = 5 \times 5 \times 2 = 50$$

Hence, tank will get filled up in 50 minutes.

or

Let AOB represent the sector of the circle with radius r = 15 cm and central angle AOB = 120° (= θ say).

Then, length of arc AB =
$$\frac{\theta}{360} \times 2\pi r$$

= $\left(\frac{120}{360} \times 2 \times \frac{22}{7} \times 15\right)$ cm = $\frac{220}{7}$ cm ...(1)

When sector is rolled up, arc AB forms the circumference of base of the cone and radius (r = 15 cm) forms the slant height of cone.

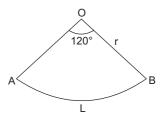
l = 15 cm

Let r_1 be the radius of cone and h its height.

...

....

$$2\pi r_1 = \frac{220}{7} \,\mathrm{cm} \quad [\mathrm{Using}\ (1)]$$



$$r_{1} = \frac{220}{7} \times \frac{1}{2} \times \frac{7}{22} = 5 \text{ cm}$$

$$h = \sqrt{l^{2} - r_{1}^{2}} = \sqrt{15^{2} - 5^{2}} = \sqrt{200} = 10\sqrt{2} \text{ cm}$$

$$h$$

$$l = r = 15 \text{ cm}$$
Volume of cone = $\frac{1}{3}\pi r_{1}^{2}h$

$$= \frac{1}{3} \times \frac{22}{7} \times (5)^{2} \times 10\sqrt{2} = 370.38 \text{ cm}^{3}.$$

Hence, the volume of the cone is 370.38 cm^3 (approx.).

35.

...

 \Rightarrow

Height	Mid value (x _i)	Number of girls (f _i)	Cumulative frequency (cf)	$f_i x_i$
120 – 130	125	2	2	250
130 - 140	135	8	10	1080
140 - 150	145	12	22	1740
150 – 160	155	20	42	3100
160 – 170	165	8	50	1320
Total	$n = \Sigma f_i = 50$			$\Sigma f_i x_i = 7490$

Mean:
$$\frac{\Sigma f_i x_i}{\Sigma f_i} = \frac{7490}{50} = 149.8$$

Median: $n = \Sigma f_i = 50$, so $\frac{n}{2} = \frac{50}{2} = 25$

Cumulative frequency just greater than 25 is 42 and the corresponding class is 150 - 160. So the median class is 150 - 160.

:.
$$l = 150, cf = 22, f = 20, h = 10$$

Median =
$$l + \left(\frac{\frac{n}{2} - cf}{f}\right) \times h$$

= $150 + \left(\frac{25 - 22}{20}\right) \times 10 = 150 + 1.5$
= 151.5

Mode: Here the maximum frequency is 20 and class corresponding to it is 150 – 160. So modal class is 150 – 160.

...

$$l = 150, f_1 = 20, f_0 = 12, f_2 = 8, h = 10$$

Mode = $l + \left(\frac{f_1 - f_0}{2f_1 - f_0 - f_2}\right) \times h$
= $150 + \left(\frac{20 - 12}{2 \times 20 - 12 - 8}\right) \times 10$
= $150 + \frac{8}{20} \times 10$
= $150 + 4 = 154$

Hence, mean height of the girls is 149.8 cm, their median height is 151.5 cm and their modal height is 154 cm.

Section - E

36. Let the sale of smartphones in 1^{st} year be a_1 and 2^{nd} year be a_2 . Difference in sale of phones in 2^{nd} year and 1^{st} year is *d*. Sale of smartphones in 3^{rd} year, $a_3 = 10,000$ Sale of smartphones in 5th year, $a_5 = 14,000$ (a) Sale in 2^{nd} year = a_2 . $a_3 = a_1 + (3 - 1)d$ $[a_n = a_1 + (n-1)d]$ $10000 = a_1 + 2d$ \Rightarrow ...(1) $a_5 = a_1 + 4d \implies 14000 = a_1 + 4d$...(2) Subtracting equation (1) from equation (2), we get $14000 - 10000 = a_1 + 4d - a_1 - 2d$ \Rightarrow $4000 = 2d \implies d = \frac{4000}{2} = 2000$ \Rightarrow $10000 = a_1 + 2 \times 2000$ $a_1 = 10000 - 4000 = 6000$ \Rightarrow

$$a_2 = a_1 + d = 6000 + 2000 = 8000$$

Hence, the sale in 2nd year is 8000.

(*b*) Total sale in first 5 years = S_5

$$S_5 = \frac{5}{2} (6000 + 14000)$$
$$= \frac{5}{2} \times 20000 = 50000$$

$$\left[S_n = \frac{n}{2}(a_1 + a_n)\right]$$

Hence, total sale of smartphones in first 5 years is 50,000.

or

Let the sale be a_n in n^{th} year. $a_n = a_1 + (n-1)d$ *.*.. $22000 = 6000 + (n - 1) \times 2000$ \Rightarrow $22000 - 6000 = (n - 1) \times 2000$ \Rightarrow $16000 = (n-1) \times 2000$ \Rightarrow $8 = n - 1 \implies n = 9$ \Rightarrow Hence, sale would be 22000 after 9th year. (c) Let the total sale will be S_n in n^{th} years. $S_n = \frac{n}{2} [2a_1 + (n-1)d]$ *.*.. $66000 = \frac{n}{2} [2 \times 6000 + (n-1) \ 2000]$ \Rightarrow $66000 = 6000n + (n^2 - n)1000$ \Rightarrow $66 = 6n + n^2 - n$ \Rightarrow $n^2 + 5n - 66 = 0$ \Rightarrow $n^{2} + 11n - 6n - 66 = 0 \implies (n - 6)(n + 11) = 0$ \Rightarrow n = 6, -11 \Rightarrow As -11 can't be possible year. Hence, total sale would be 66,000 after 6 years. 37. (a) Coordinates of C is (-5, -3), A is (2, 7), B is (7, -8) By distance formula = $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$ Distance between A and C = $\sqrt{(2+5)^2 + (7+3)^2}$ $= \sqrt{49 + 100} = \sqrt{149}$ unit Distance between B and C = $\sqrt{(7+5)^2 + (-8+3)^2}$ $= \sqrt{144 + 25} = \sqrt{169} = 13$ unit Hence, Dev travelled more distance.

30

(b) By mid-point formula coordinates of mid-point of BA is (x, y)

$$x = \frac{7+2}{2}, y = \frac{-8+7}{2} \qquad \left[x = \frac{x_1 + x_2}{2}, y = \frac{y_1 + y_2}{2} \right]$$
$$x = \frac{9}{2}, y = -\frac{1}{2}$$
Hence, coordinates of that place is $\left(\frac{9}{2}, -\frac{1}{2}\right)$

or

Area of triangle formed by points A, B and C is ABC

$$= \frac{1}{2} [x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)]$$

$$= \frac{1}{2} |2(-8 - 7) + 7(-3 - 7) + (-5) (7 + 8)|$$

$$= \frac{1}{2} |2(-15) + 7(-10) - 5 \times 15|$$

$$= \frac{1}{2} (-30 - 70 - 75)$$

$$= \frac{1}{2} (-175) = 87.5 \text{ sq units.}$$

Hence, area of the triangle formed by A, B and C is 87.5 unit square.

(c) Distance between A and B = $\sqrt{(7-2)^2 + (-8-7)^2}$

=
$$\sqrt{25 + 225}$$

= $\sqrt{250}$ unit = $5\sqrt{10}$ unit

38. Let AE be height of the tree and BD is height of the tower.

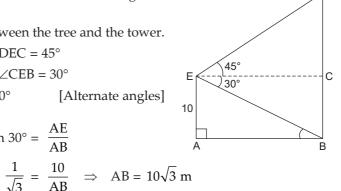
AB is the distance between the tree and the tower.

Angle of elevation, $\angle DEC = 45^{\circ}$

Angle of depression, $\angle CEB = 30^{\circ}$

(*i*) $\angle ABE = \angle CEB = 30^{\circ}$ [Alternate angles] In $\triangle AEB$,

 $\tan 30^\circ = \frac{AE}{AB}$



D

 \Rightarrow

Therefore, distance between the tree and the tower = $10\sqrt{3}$ m (*ii*) In $\triangle CDE$,

$$\tan 45^\circ = \frac{\text{CD}}{\text{EC}}$$

$$\Rightarrow \qquad 1 = \frac{CD}{10\sqrt{3}} \qquad [EC = AB]$$

$$\Rightarrow \qquad CD = 10\sqrt{3} m$$

$$\therefore \qquad BD = BC + CD = 10 + 10\sqrt{3} = 10 (1 + \sqrt{3}) m$$
Therefore, height of the tower = 10 (1 + $\sqrt{3}$) m
Area of trapezium ABDE = $\frac{1}{2} \times [\text{sum of lengths of parallel sides} \times \text{distance between them}]$

$$= \frac{1}{2} [10 + 10(1 + \sqrt{3})] \times 10\sqrt{3} m^{2}$$

$$= [20 + 10\sqrt{3}] \times 5\sqrt{3} = (100\sqrt{3} + 150) m^{2}.$$
or
$$\sin 45^{\circ} = \frac{CD}{ED}$$

$$\Rightarrow \qquad \frac{1}{\sqrt{2}} = \frac{10\sqrt{3} m}{ED}$$

$$\Rightarrow \qquad ED = 10\sqrt{6} m$$
Perimeter of the trapezium = AB + BD + ED + AE
$$= (10\sqrt{3} + 10 + 10\sqrt{3} + 10\sqrt{6} + 10) m$$

$$= (20 + 20\sqrt{3} + 10\sqrt{6}) m$$

$$\therefore \quad \text{Perimeter of the trapezium = 10(2 + 2\sqrt{3} + \sqrt{6}) m.$$

Hence, perimeter of the trapezium is $10(2 + 2\sqrt{3} + \sqrt{6})$ m.

(*iii*) Height of the tower = BC + CD = $10 + 10\sqrt{3}$

 $= 10(1 + \sqrt{3})$ m.

Hence, height of the tower = $10(1 + \sqrt{3})$ m.